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Course: II year MSC (Maths)

#### Paper – I Topology and Functional Analysis

#### **Question Paper for Assignment**

Answer any <u>THREE</u> of the following <u>FIVE</u> Questions.

3x10=30

- 1. a) Let X be a Topological space and  $A \subset X$  prove
  - That (1)  $\bar{A} = A \cup D(A)$ 
    - (2) A is closed iff  $A \supset D(A)$
  - b) State and prove Lindelof Theorem
- 2. a) State and prove Tychonff's Theorem and Heine Borel Theorem?
  - b) Prove that a topological space is compact if every basic open cover has a finite subcover?
- 3. a) Prove that Letm be a closed Linear subspace of a Normed Linear space N. If the nom of a coset x + M in the quotient space N/M is defined by  $\|x + M\| = Inf\{\|x + m\| \colon m \in M\}$  the  $\frac{N}{M}$  is a Normed space. Further move if N is a

Banach space. Then N/M is a Banach Space?

- b) State and prove Hahn Banach theorem?
- 4. a) State and Prove closed graph Theorem?
  - b) State and Prove open mapping Theorem?
- 5. a) State and Prove uniform Boundedness Theorem?
  - b) Let T be an operator on a Banach space B. Then T has an Inverse  $T^{-1}$  if any if  $T^*$  has an Inverse  $(T^*)^{-1}$  and  $(T^*)^{-1} = (T^{-1})^*$

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Paper – II Measure and Integration

# **Question Paper for Assignment**

Answer any <u>THREE</u> of the following <u>FIVE</u> Questions.

3x10=30

- 1. (a) Define a Equivalence relation. Axiom of choice, Zorm'slex?
  - (b) Define a Borel set and prove that for a set of real numbers E. its closure  $\underset{E}{\leftrightarrow}$  is closed set that contains E in the sense that if F is closed and E  $\leq$  F. Then  $\underset{E}{\leftrightarrow} \leq$  F?
- (a) Define a outer measure. Prove that every outer measure is its length?
  - (b) State and prove countable subadditivity?
- 3. (a) Prove that f is measure function and **F = g** a.e then g is measurable?
  - (b) State and prove Egoroff's theorem?
- 4. (a) State and prove Bounded Convergence theorem?
  - (b) Let f be a bounded function defined on [a,b] if f is primann Integrable on [a,b]. Then it is measurable and R  $\int_a^b f \ dx = \int_a^b f \ dx$ ?
- 5. (a) State and prove Fatou's lemma?
  - (b) State and prove monotenic Convergence theorem?



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#### Paper – III Analytic Number Theory (or) Discreate Mathematics

# **Question Paper for Assignment**

Answer any <u>THREE</u> of the following <u>FIVE</u> Questions.

3x10=30

- 1. (a) Define a Euler's Constant?
  - (b) State and Prove Euler's Summation formula?
- 2. (a) For All  $x \ge 1$  Prove that  $\sum d(n) + x \log x + (2c 1)x + 0(\sqrt{x}) n \le x$ 
  - (b) State and Prove Legendre's Identity?
- 3. Prove that for every Integer  $n \ge 2$ , we have  $\frac{1}{6} \frac{n}{logn} < \pi(n) < 6 \frac{n}{Log n}$
- 4. State and Prove Selberg's Asymptotic Formula?
- 5. State and Prove Shapiro's Tauberian Theorem?

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# Paper – IV Computer Algorithm and Problems Solving

# **Question Paper for Assignment**

Answer any <u>THREE</u> of the following <u>FIVE</u> Questions.

3x10=30

- 1. Write an algorithm of Fibonacci sequence?
- 2. Draw a flowchart of Fibonacci sequence?
- 3. Write an algorithm that accepts a positive integer and reverses the order of its digits?
- 4. Write an algorithm to a given randomly ordered array of n elements?
- 5. Define the constructor of loops and Termination of loops?

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Paper – V

#### C and Data Structures

# Question Paper for Assignment

Answer any <u>THREE</u> of the following <u>FIVE</u> Questions.

3x10=30

- 1. (a) Write the Syntax of loop operations provide in the C languages?
  - (b) Write a Program using while loop to reverse the digits of the given number?
- 2. (a) Explain about 'C' language character set?
  - (b) Give an explanation about increment and Decrement Operators?
- 3. (a) Explain about Storage Classes?
  - (b) About in a Multi- Dimensional array? Give Syntax of Multi Dimensional array?
- 4. (a) Write down the differences between library functions and user defined functions?
  - (b) Write a program using a single subscripted variable to evaluate the following Expressions:

Total= 
$$\sum_{i=1}^{10} x^2$$

The values of  $X_1X_2$  -----,  $X_{10}$  are read from the terminal.

- 5. (a) What are the benefits of Points to the C Programmers?
  - (b) Write a program using pointers to complete the sum of all elements stored in an array?